

A radical breach with Aristotle

The European Research Council (ERC) is funding research into contradictory logics with two million euros.



Figure 1: Adobe Stock: Aristotle © Worldillustrator. Generated with AI.

For Aristotle, it was the most certain of all principles and needed no further justification: no declarative sentence (or proposition or statement) is both true and false. If the negation of a proposition expresses its falsity, and the proof of a proposition guarantees its truth, then it should be impossible for proposition *A and its negation*, ~*A*, both to be provable.

An international team of researchers led by Professor Heinrich Wansing at the Ruhr University Bochum (Germany) is radically breaking with Aristotle and researching logical systems that contain provable contradictions. The project 'Contradictory Logics: A Radical Challenge to Logical Orthodoxy' (ConLog), cordis. europa.eu/project/id/101018280, is funded by the ERC with a two million euro ERC Advanced Grant. The ERC's mission is to fund "high-risk/high-gain research". The benefit of a project is expected to be so high that it is worth the considerable risk taken in carrying it out. The risk for the ConLog project appears to be very high indeed, and its goals are ambitious. As Nicholas Rescher and Robert Brandom (The Logic of Inconsistency, Basil Blackwell, Oxford, 1980) remarked:

Similarly, the philosopher of science, Sir Karl Popper, was of the opinion that "the acceptance of contradictions... must lead to the end of all criticism and to the collapse of science" (Conjectures and Refutations: The Growth of Scientific Knowledge, Routledge, London, 1962). The provability of contradictions would thus have an absolutely disastrous effect on science. Supporters of the so-called "classical logic" developed by mathematicians and philosophers such as George Boole, Gottlob Frege and Bertrand Russell must agree with Popper's diagnosis. According to classical logic, arbitrary statements follow from contradictory assumptions: *ex* contradictione quodlibet. Contradictions trivialise theories, and scientists should, therefore, avoid contradictions at all costs. But this view had already begun to erode in the 20th century. Logicians and philosophers such as Stanisław Jaśkowski, Newton da Costa and Graham Priest developed so-called 'paraconsistent' systems of logic, for which ex contradictione quodlibet does not hold. The formulation and application of paraconsistent logics can be seen as an important step in the history of ideas. Professor Wansing's team goes one step further and investigates logics on the basis of which every regular theory, i.e. statements of the theory, is contradictory.



Professor Graham Priest, City University of New York and International Research Fellow at Ruhr University Bochum: There are true contradictions.

What is a contradiction?

A contradiction is often understood to be the conjunction of a proposition and its negation, which shifts much of the discussion of provable contradictions to the notion of negation.

What is negation?

The answer to the question is controversial, but the logical systems considered in the ConLog project make use of established notions of negation, so that indeed provable contradictions are under consideration.

Professor Wansing's research team is trying to gain a deeper understanding of these provable contradictions. The logics investigated are not ad hoc and have not been fabricated artificially just in order to obtain examples of non-trivial contradictory logics. Rather, it turns out that it is possible to arrive at nontrivially contradictory, so-called 'negation inconsistent' logics in a completely natural way. A key to understanding certain such logics is what the Mexican philosopher Luis Estrada-González has called The Bochum Plan, alluding to the investigations at the Ruhr University Bochum. Unconventional, but by no means unnatural, conceptions

Since Aristotle's days, virtually all logicians and logically concerned philosophers in the mainstream of the Western tradition have had a phobia of inconsistency. They have been near to unanimous in proscribing it from the precincts of their logical and ontological theorising, holding that toleration of inconsistencies would inevitably bring cognitive disaster in its wake."

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It is largely uncontroversial to derive the conjuncts A and B from a conjunction A and B (A & B). Accordingly, both A and A & \sim A, and thus the statements If (A & ~A), then A (abbreviated as (A & ~A) \rightarrow A) from classical logic, that an implication *If* A, then B is falsified just in case If A, then ~B is verified, then the negation ~((A & $\sim A$) $\rightarrow A$) of (A & $\sim A$) $\rightarrow A$) says as much as $(A \& \neg A) \rightarrow \neg A$ and the two contradictory statements (A & $\sim A$) $\rightarrow A$ and \sim ((A & $\sim A$) $\rightarrow \sim A$) are both provable.

contradictions, it seems necessary to develop a fundamentally new understanding of logic. For the founder of modern formal logic, Gottlob Frege, of being true", and with the Aristotelian avoids a metaphysical commitment to banishment of contradictions, it is then the existence of *true* contradictions.

the laws of being true is contrasted by provable. If it is now assumed, in deviation is inescapably given. While Priest advocates a metaphysical theory of socalled 'dialetheism', according to which there are true contradictions, Wans that certain contradictory information is unavoidable. Both approaches propagate paraconsistency: it is by no means the To make sense of the provability of case that arbitrary statements follow from contradictory assumptions, and the banishment of all contradictions for fear However, the view that logic is dedicated logic investigates "the most general laws to the study of the flow of information

PROJECT NAME

Contradictory Logics: A Radical Challenge to Logical Orthodoxy (ConLog)

PROJECT SUMMARY

ConLog investigates non-trivial logical systems in which certain contradictions are provable. The aim is to develop a clear comprehension of the contradictoriness of these logics and to study the consequences of this understanding within the philosophy of logic. Thereby, the project will yield a paradigm shift in our conception of what a respectable logical system and an acceptable scientific theory is.

PROJECT LEAD PROFILE

Heinrich Wansing is a professor of Logic and Epistemology at the Ruhr University Bochum. Before that, he was a professor at TU Dresden (1999-2010). He is the (co-) author of five monographs and numerous articles on topics from philosophical logic. Moreover, he is the editor-in-chief of the book series Trends in Logic (Springer) and a managing editor of the journal Studia Logica.

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Professor Heinrich Wansing, **Ruhr University Bochum:** There are provable contradictions.



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